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Subcritical approximation of a Yamabe-type nonlocal equation: a Gamma-convergence approach

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Abstract. We investigate a natural approximation by subcritical Sobolev embeddings of the Sobolev quotient for the fractional Sobolev spaces H^s for any 0 < s < N/2, using Γ -convergence techniques. We show that, for such approximations, optimal functions always exist and exhibit a concentration effect of the H^s energy at one point.

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