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Quaternionic maps and minimal surfaces

JINGYI CHEN AND JIAYU LI

Abstract. Let $(M, J^{\alpha}, \alpha = 1, 2, 3)$ and $(N, \mathcal{J}^{\alpha}, \alpha = 1, 2, 3)$ be hyperkähler manifolds. We study stationary quaternionic maps between M and N. We first show that if there are no holomorphic 2-spheres in the target then any sequence of stationary quaternionic maps with bounded energy subconverges to a stationary quaternionic map strongly in $W^{1,2}(M, N)$. We then find that certain tangent maps of quaternionic maps give rise to an interesting minimal 2-sphere. At last we construct a stationary quaternionic map with a codimension-3 singular set by using the embedded minimal \mathbb{S}^2 in the hyperkähler surface \widetilde{M}_2^0 studied by Atiyah-Hitchin.

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