Ann. Sc. Norm. Super. Pisa Cl. Sci. (5) Vol. XXII (2021), 835-852

## Homology of the Lie algebra $\mathfrak{gl}(\infty, R)$

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Dedicated to the memory of our friend Jean-Louis Loday

**Abstract.** In this note we compute the homology of the Lie algebra  $\mathfrak{gl}(\infty, R)$  where *R* is an associative unital *k*-algebra which is used in higher dimensional soliton theory [19]. When *k* is a field of characteristic 0, our result justifies an old result of Feigin and Tsygan [5]. The special case when  $R = k = \mathbb{C}$  appeared first in soliton theory (*cf.* [9]).

Mathematics Subject Classification (2010): 17B65 (primary); 16S35, 16E40 (secondary).